# University Defence Research Collaboration (UDRC) Signal Processing in a Networked Battlespace

L\_WP2: Handling uncertainty and incorporating domain knowledge (Loughborough University)

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L\_WP2.1 Reducing uncertainty by incorporating domain knowledge using Bayesian inference and adaptive signal processing

#### **Objectives**

- A framework to explore all the previously collected information and data available for moving platforms in a networked environment when performing signal process will be developed.
- New signal processing algorithms offering adaptivity to operational environments will be developed by exploiting domain knowledge.
- Extension will be made to multiple sensor platforms operating in a networked environment by fusing different types of information.

# **General Tracking Problem**

Aim: Obtaining a Minimum Mean Square Error estimator (MMSE) and its confidence



### L\_WP2.2: Game Theoretic Framework for Radar Waveform Design

# Objectives

- Understand uncertainties caused deliberately by intelligent targets equipped with jammers, and develop game theoretic methods for radar waveform design that is robust against jamming.
- Enhance the defence against jamming within a radar network environment through the distributed resource allocation and waveform design, with a focus on MIMO radars.

# MIMO Radars

**Phased Arrays:** 

- Coherent beam
- High antenna gain (good SNR)
- Good detection performance in low SNR

MIMO (Multiple-Input-Multiple-Output) Radar:



State model:  $x_k = f(x_{k-1}, v_k) \sim p(x_k | x_{k-1})$ Measurement model:  $y_k = h(x_h, e_k) \sim p(y_k | x_k)$ 

- $x_k$ : state variable representing the state (position, velocity) of a vehicle
- $y_k$ : observation from different types of sensors

# **Bayesian Inference Scheme**

Estimate both the posterior mode probability  $p(r_k|y_{1:k})$  and the MMSE  $E(x_k|r_k, y_{1:k})$  based on  $p(x_k|r_k, y_{1:k})$ , where  $r_k$  represents the mode.

It divides into three steps:

- Estimating the initial mode conditioned probability  $p(x_{k-1}|r_k, y_{1:k-1})$
- > Estimating  $p(x_k | r_k, y_{1:k})$  using a filtering particle scheme such as an auxiliary particle filter
- > Calculating the posterior mode probability  $p(r_k|y_{1:k})$

#### **Domain Knowledge**

- Road geometry information: the movement of the vehicle is constrained by the shape of the road.
- Expert knowledge information: the movement of the vehicle is constrained by the properties of a road segment.

#### **Simulated Scenario**





Auxiliary Particle Filter Scheme



- A UAV is simulated to circle around for monitoring the corresponding area.
- A vehicle moves on the ground with different types of manoeuvre.

- Transmission of independent signals (waveform diversity)
- Detection of slow moving targets



Improved parameter identifiability

#### **Game Theory**

<u>Game theory</u> provides the means to model, analyse and understand situations involving interactions among various decision-makers.

- > A game G is a tuple  $< N, (A_i), (u_i) >$ , where
  - N is a set of players
  - $A_i$  is a set of actions associated with each player i
  - $u_i$  is a payoff function, which represents the players' preferences on the actions
- The solution of a game is a systematic description of the outcomes that may emerge in a family of games.



**Nash equilibrium** is the action profile such that no player can profitably deviate from their strategy.

John Forbes Nash, Jr.

# **Current Research Direction**

Game theoretic framework for beamforming design for a radar network with power constraints, where the beamforming is considered in transmission and reception.

- > The radars in the network aim to detect the same target.
- Each radar acts independently (non-cooperative game).
- > Each radar should not deliberately interfere with the signal of the other radars.
- The radars have limited power.

Bayesian inference scheme is applied and domain knowledge is incorporated to improve the performance.

#### **Future Works**

- Scenarios: More complicated scenarios like a vehicle moving both on and off road in battlefield, and urban environment will be studied.
- Algorithms: More advanced algorithms to enhance both the accuracy and efficiency (e.g. particle swarm optimization (PSO) based particle filtering method) will be investigated.
- Knowledge: More types of domain knowledge, such as the available information from the GIS system, will be applied.

#### Future Works

#### <u>Case 1</u>

Players: network of phased-array

**Aim**: achieve good detection performance while keeping interference at low levels

**Strategy**: beamforming design, power allocation

**Payoff**: SINR, probability of false alarm and miss-detection

<u>Case 2</u>

**Players**: network of MIMO radars vs intelligent target equipped with a jammer

#### Aim:

Radar: maximize detection performance

**Target**: deliberate interference to minimize detection performance

**Strategy**: waveform design, power allocation

**Payoff:** SINR, probability of false alarm and miss-detection



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