







Source Dependency Modelling in Frequency Domain Source Separation

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• IVA application on iPhone



[1] N. Ono, "Blind source separation on iPhone in real environment," in EUSIPCO 2013, Marrakech, Morocco, 2013.





- 1. Blind Source Separation (BSS)
- 2. Independent Vector Analysis (IVA)
- 3. Copula Based Dependency Model
- 4. IVA with Multivariate Student's t Source Prior
- 5. Experimental Results
- 6. Conclusions



Blind Source Separation



"One of our most important faculties is our ability to listen to, and follow, one speaker in the presence of others. This is such a common experience that we may call it 'the cocktail party problem.' No machine has been constructed to do just this, to filter out one conversation from a number jumbled together...".



Colin Cherry 1914-1979





Blind Source Separation



Independent component analysis (ICA) is the central tool for BSS, which is a higher order statistic method.

ICA has two ambiguities

- 1. The scaling ambiguity
- 2. The permutation ambiguity







The cost function for IVA is the Kullback-Leibler divergence between the joint probability density function and the product of marginal probability density functions of the individual source vectors [1].

$$J = \mathcal{KL}\left(p(\hat{\mathbf{s}}_1 \dots \hat{\mathbf{s}}_N) || \prod p(\hat{\mathbf{s}}_i)\right)$$

= $\int p(\hat{\mathbf{s}}_1 \dots \hat{\mathbf{s}}_N) \log \frac{p(\hat{\mathbf{s}}_1 \dots \hat{\mathbf{s}}_N)}{\prod q(\hat{\mathbf{s}})} d\hat{\mathbf{s}}_1 \dots d\hat{\mathbf{s}}_N$
= $const - \sum_{k=1}^K \log |det(W(k))| - \sum_{i=1}^N E[\log p(\hat{\mathbf{s}}_i)]$



[2] T. Kim, H. Attias, S. Lee, and T. Lee, "Blind source separation exploiting higher-order frequency dependencies," *IEEE Transactions on Audio, Speech and Language processing*, vol. 15, pp. 70–79, 2007.



The natural gradient IVA:

$$W(k)_{new} = W(k)_{old} + \eta \Delta W(k)$$
$$\Delta W(k) = \left(\mathbf{I} - E[\varphi^{(k)}(\hat{s})\hat{s}^*(k)]\right)W(k)$$
$$\varphi^{(k)}(\hat{s}) = [\varphi^{(k)}(\hat{s}_1), \cdots, \varphi^{(k)}(\hat{s}_N)]^T$$
$$\varphi^{(k)}(\hat{s}_i) = -\frac{\partial \log p(\hat{s}_i)}{\partial \hat{s}_i(k)}$$

Original source prior for IVA:

Original score function for IVA:





• Fast fixed point IVA The cost function:

$$J_{FastIVA} = \sum_{i=1}^{N} \left(E[F(\sum_{k=1}^{K} |\hat{s}_i(k)|^2)] - \sum_{k=1}^{K} \lambda_i(k) (\mathbf{w}_i(k)^{\dagger} \mathbf{w}_i(k) - 1) \right)$$

The updates rules:

$$\mathbf{w}_{i}(k) \leftarrow E[F'(\sum_{k'=1}^{K} |\hat{s}_{i,o}(k')|^{2}) + |\hat{s}_{i,o}(k)|^{2}F''(\sum_{k'=1}^{K} |\hat{s}_{i}(k')|^{2}))]\mathbf{w}_{i}(k) - E[(\hat{s}_{i,o}(k))^{*}F'(\sum_{k'=1}^{K} |\hat{s}_{i,o}(k')|^{2})\mathbf{x}(k)]$$

$$W(k) \leftarrow (W(k)(W(k))^{\dagger})^{-1/2}W(k).$$

- Auxiliary function based IVA Auxiliary function technique
 - $$\begin{split} \bar{\Theta} &= argmin_{\Theta}J(\Theta)\\ J(\Theta) &= min_{\tilde{\Theta}}Q(\Theta,\tilde{\Theta})\\ \tilde{\Theta}(i+1) &= argmin_{\tilde{\Theta}}Q(\Theta(i),\tilde{\Theta})\\ \Theta(i+1) &= argmin_{\Theta}Q(\Theta,\tilde{\Theta}(i+1)) \end{split}$$

The update rules:

$$\begin{aligned} r_i &= \sqrt{\sum_{k=1}^{K} |\mathbf{w}_i^{\dagger}(k) \mathbf{x}(k)|^2} \\ V_i(k) &= E\left[\frac{g'_R(r_i)}{r_i} \mathbf{x}(k) \mathbf{x}(k)^{\dagger}\right] \\ \mathbf{w}_i(k) &= (W(k) V_i(k))^{-1} \mathbf{e}_i \\ \mathbf{w}_i(k) &= \frac{\mathbf{w}_i(k)}{\sqrt{\mathbf{w}_i^{\dagger}(k) V_i(k) \mathbf{w}_i(k)}} \end{aligned}$$



• Sklar's Theorem:

$$F(z_1,\cdots,z_d)=C(F_1(z_1),\cdots,F_d(z_d))$$

• Copula density function:

$$c(\boldsymbol{u}) = \frac{\partial^d C(u_1, \cdots, u_d)}{\partial u_1 \cdots u_d}$$

• The joint probability density function:

$$p(z_1, \cdots, z_d) = \frac{\partial^d F(z_1, \cdots, z_d)}{\partial z_1 \cdots z_d}$$
$$= \frac{\partial^d C(F_1, \cdots, F_d)}{\partial F_1 \cdots F_d} \frac{\partial F_1}{\partial z_1} \cdots \frac{\partial F_d}{\partial z_d}$$
$$= c(F_1, \cdots, F_d) \prod_{i=1}^d p_i(z_i)$$



• T copula

$$C(u) = \int_{-\infty}^{F_1^{-1}} \cdots \int_{-\infty}^{F_d^{-1}} \frac{\Gamma(\frac{v+d}{2})}{\Gamma(\frac{v}{2})(\sqrt{\pi v |\Sigma|})} (1 + \frac{z^{\dagger} \Sigma^{-1} z}{v})^{-\frac{v+d}{2}} dz$$

• T copula density function

$$c(u_1, \cdots, u_d) = \frac{\Gamma(\frac{v+d}{2})\Gamma(\frac{v}{2})^{d-1}}{|\Sigma|^{\frac{1}{2}}\Gamma(\frac{v+1}{2})^d} \frac{\prod_{i=1}^d (1 + \frac{|z_i|^2}{v})^{\frac{v+1}{2}}}{(1 + \frac{z^{\dagger}\Sigma^{-1}z}{v})^{\frac{v+d}{2}}}$$

• T copula density function with four degrees freedom and 0.7 correlation coefficient.





• T copula density function with four degrees freedom and -0.6 correlation coefficient.



T copula density function with four degrees freedom and zero correlation coefficient.





 The calculations of Chi and lamda • for Chi plot [2]

$$\tilde{H}_i = \sum_{j \neq i} I(x_j \le x_i, y_j \le y_i) / (n-1)$$

$$\tilde{F}_i = \sum_{j \neq i} I(x_j \le x_i) / (n-1)$$

$$\tilde{G}_i = \sum_{j \neq i} I(y_j \le y_i) / (n-1)$$

$$\tilde{S}_i = sign[(\tilde{F}_i - 0.5)(\tilde{G}_i - 0.5)]$$

Scatter plot and Chi plot of two independent random variables



 $Chi_{i} = (\tilde{H}_{i} - \tilde{F}_{i}\tilde{G}_{i})/\sqrt{\tilde{F}_{i}(1 - \tilde{F}_{i})\tilde{G}_{i}(1 - \tilde{G}_{i})}$ $lamda_{i} = 4S_{i}max((\tilde{F}_{i} - 0.5)^{2}, (\tilde{G}_{i} - 0.5)^{2})$

In Chi plot, if all the points are between the two lines, it means independent, otherwise dependent.

[3] N. I. Fisher and P. Switzer, "Chi-plots for assessing dependence," Biometrika, vol. 72, pp. 253-265, 1985.



Two correlated variables with a t copula 2 2 Chi -0.8 -0.6 -0.4 0.8 0.4 0.6 -0.2 0 02 lamda

Two uncorrelated variables with a t copula





The Chi plots of two frequency bins of a speech signal, i.e. 50th and 51th frequency bins, 50th and 55th frequency bins, 50th and 60th frequency bins, 50th and 100th frequency bins, 50th and 200th frequency bins, 50th and 500th frequency bins.





IVA with Multivariate Student's t Source Prior

• Assuming the marginal distribution for the t copula is a student's t distribution:

$$p(s_i(k)) = \frac{\Gamma(\frac{v+K}{2})}{\sqrt{v\pi}\Gamma(\frac{v}{2})} (1 + \frac{|s_i(k)|^2}{v})^{-\frac{v+1}{2}}$$

• The multivariate student's t source prior:

$$p(\mathbf{s}_i) \propto (1 + \frac{\sum_{k=1}^{K} |s_i(k)|^2}{v})^{-\frac{v+K}{2}}$$

• The new nonlinear score function:

$$\varphi^{(k)}(\hat{s}_i(1)\cdots\hat{s}_i(k)) = \frac{v+K}{v} \frac{\hat{s}_i(k)}{1+\frac{1}{v}\sum |\hat{s}_i(k)|^2}$$





Experimental Results

Different speech signals are selected from the TIMIT dataset, and convolved into mixtures. The reverberation time RT60 is set to be 200ms.

| mixtures | original(dB) | proposed(dB) | improvement(dB) |
|-----------|--------------|--------------|-----------------|
| mixture1 | 18.81 | 20.12 | 1.31 |
| mixture2 | 15.94 | 17.26 | 1.32 |
| mixture3 | 9.97 | 11.73 | 1.76 |
| mixture4 | 11.68 | 12.40 | 0.72 |
| mixture5 | 18.80 | 19.91 | 1.11 |
| mixture6 | 12.27 | 18.74 | 6.47 |
| mixture7 | 8.88 | 11.10 | 2.22 |
| mixture8 | 15.57 | 17.09 | 1.52 |
| mixture9 | 18.10 | 19.50 | 1.4 |
| mixture10 | 16.84 | 19.65 | 2.81 |

TABLE I

SEPARATION PERFORMANCE COMPARISON IN SDR

TABLE II

SEPARATION PERFORMANCE COMPARISON IN SIR

| mixtures | original(dB) | proposed(dB) | improvement(dB) |
|-----------|--------------|--------------|-----------------|
| mixture 1 | 20.30 | 21.43 | 1.13 |
| mixture2 | 17.88 | 19.00 | 1.12 |
| mixture3 | 12.08 | 12.77 | 0.69 |
| mixture4 | 14.42 | 14.97 | 0.55 |
| mixture5 | 20.28 | 20.95 | 0.67 |
| mixture6 | 14.08 | 20.94 | 6.86 |
| mixture7 | 10.72 | 12.57 | 1.85 |
| mixture8 | 16.98 | 18.77 | 1.79 |
| mixture9 | 20.14 | 20.80 | 0.66 |
| mixture10 | 19.53 | 21.54 | 2.01 |

50 different speech mixtures are tested, and the average SDR and SIR improvements are 1.3 dB and 1.1 dB respectively.



Experimental Results

• Performance in different room environments





Experimental Results

• Experiments by using real room recordings.

TABLE III

SEPARATION RATE COMPARISON WHEN USING REAL ROOM RECORDINGS

| | mixtures | original | proposed |
|-----------------|----------|----------|----------|
| separation rate | 0.0379 | 0.2515 | 0.2794 |









Conclusions

- The dependency structure within the frequency domain speech signals was exploited by introducing copula theory.
- The t copula was found suitable to model the inter-frequency dependency, which was also confirmed by observing the Chi-plot between two frequency bins of a real speech signal.
- A multivariate student's t distribution was constructed by using the t copula density function and univariate student's t marginal distribution, which was adopted as the new source prior for the NG-IVA algorithm.
- The separation performance was tested in different reverberant room environments and also by using real room recordings. The average SDR and SIR improvement are approximately 1.3dB and 1.1dB respectively.



References

[1] N. Ono, "Blind source separation on iPhone in real environment", EUSIPCO 2013, Marrakech, Morocco, 2013.

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Thanks for your attention!

Questions?

