# WP 1.1

Scalable Solutions for Probabilistic Modelling and Uncertainty Quantification

- · Academics: Y. Altmann, Y. Wiaux, S. McLaughlin, M. Davies,
- PDRA:
  - Ahmed K. Eldaly (July 2019-Dec. 2021)
- Associated PhDs:
  - Dan Yao (until Oct. 2021)
  - Kristofer Drummond (CENSIS/Leonardo, since Jan. 2020)





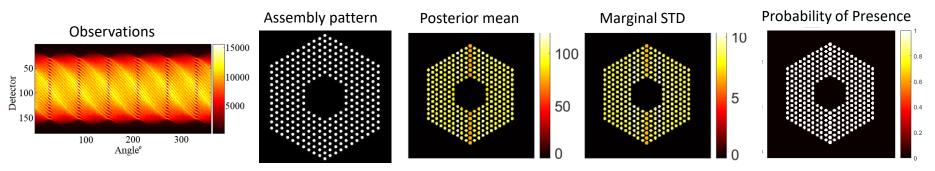
### Aims and objectives of the work package

- Development of tools for uncertainty quantification for large-scale inverse problems
- Typical challenges:
  - High-dimensional and/or multimodal imagery
  - Highly ill-posed problems (noisy measurement, compressed data,...)
  - Non standard noise statistics
- Methods investigated
  - High-dimensional Markov chain Monte Carlo (MCMC) methods
  - Approximate Bayesian methods (variational inference)
  - Bayesian filters for dynamic problems

### Uncertainty Quantification (UQ) via simulation methods

Activity Estimation and Uncertainty Quantification for Passive Gamma Emission Tomography

- Poisson and Gaussian noise models
- Hierarchical Bayesian model with different image priors
- Bayesian inference using MCMC
  - Posterior means and uncertainty quantification (marginal variances)



A. K. Eldaly et al. "Bayesian Activity Estimation and Uncertainty Quantification for Passive Gamma Emission Tomography", J. of Imaging, 2021.

### Approximate inference for scalable UQ

Observation y

EP-EM

- **Expectation-Propagation for** • linear inverse problem
  - Patch-based and non-convex • image priors
  - Hyperparameter estimation • SK-ROCK (on-going).
  - Application to deconvolution •

VB





PSNR: 25.48 dB

PSNR: 18.48 dB

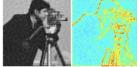


PSNR: 22.97 dB

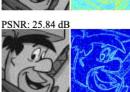
PSNR: 22.97 dB

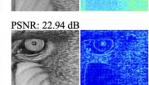


PSNR: 23.93 dB



PSNR: 24.34 dB

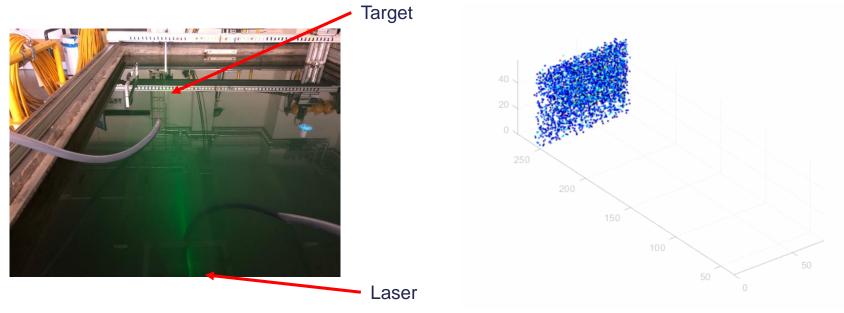




- D. Yao et al., "Patch-Based Image Restoration using Expectation-Propagation", SIAM J. Imaging Sci., 2021, to appear.
- D. Yao et al., "Fast Scalable Image Restoration using Total Variation Priors and Expectation-Propagation", 2021, submitted (available on arxiv)

# Scalable 3D imaging

- Real-time implementation
  - Algorithm comparison (10fps)
  - Underwater experiments (3.4m) Single-photon group (HWU)



- Collaborations with Leonardo UK and MBDA
- Kris Drummond et al., "Joint surface detection and depth estimation from single-photon Lidar data using ensemble estimators", SSPD 2021, Edinburgh.
- J. Tachella et al., "Real-time 3D reconstruction from single-photon Lidar data using plug-and-play point cloud denoisers", Nature Comm., 2019.