# University Defence Research Centre (UDRC) In Signal Processing

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[C1/C6] Autocalibration and Flexible Array Signal Processing Theme: Detection, Localisation & Tracking Theme *PI: Prof. A. Manikas, Imperial College London Researchers: M. Willerton* 

## **Project Objectives**

- Analyse uncertainties and their effect in an array system
- Develop pilot, self and hybrid calibration algorithms to perform smart, online and automatic calibration of the array
- Investigate flexible array systems
- Develop flexible array signal processing techniques for detection, localisation and tracking in wideband or narrowband environments

# **Array Calibration**

• **Problem**: Array systems contain different types of uncertainties such as electrical (i.e. gain, phase, coupling effects) and geometrical which affect the performance of an array system

## **Flexible Array Signal Processing**

- **Problem**: Array shape may be a time varying function
- Aim: Develop algorithms to track array shape over time
- Approaches employed in this project:
  - 1. Eigenvector based methods
  - Slow varying geometries
  - Partition data in to time frames
  - Using the engine as a source, construct second order statistics of array data to estimate range of the engine to each of the array elements
  - In R<sup>2</sup> space either:
    - Use another transmitter (pilot or transmitter on the towed array)
       Assume sensor spacing remains fixed

Applications include towed arrays

## Aim: Develop algorithms to estimate the array uncertainties

#### Approaches employed in this project:

- 1. Express planar array as a Virtual Uniform Linear Array
- 2. Pilot calibration single or multiple frequencies
- 3. Self calibration using Biogeography Based Optimisation
- 4. Autocalibration allowing array elements to operate as transceivers

#### Array Autocalibration



- Transmitters in arrays near-far field
- Spherical wave propagation
- Range and direction parameters
- Rotate array reference point



### <u>Autocalibration Example – MUSIC algorithm performance</u>

 N=6 Sensor Uniform Circular Array with gain, phase and 2D geometrical uncertainties. Calibrate assuming M=2 array elements can transmit.



Azimuth in Degree



## 2. State space based methods

- Array geometry may now change on a snapshot by snapshot basis
- Devised state space model to "filter out" array uncertainties by solving a H<sup>∞</sup> optimisation problem. The array can then be seen as static
- The state space model may also be used to estimate the true direction of a pilot source if it contains errors (before a pilot calibration or eigenvector based flexible array approach is applied)

Eigenvector Example – Array elements towed in an arc at different speeds

- Gain, phase and location uncertainties with array moving in a circular arc
- RMSE of sensor locations after the proposed approach degrades as the array moves faster
- Engine and another source along the towed array transmit



second source (along line at known direction to engine)

 $\rho_{ei}$ 

 $i^{th}$  sensor

 $ho_{si}$ 

10-1000Hz

Engine (first source)

wideband tones

MUSIC spectrum for 3 sources at 30°, 35° and 120° RMSE for 1 source at 30° azimuth using MUSIC over azimuth under L=100 snapshots and SNR=30dB 200 realizations

- [1] Y.I. Kamil, A. Manikas and M. Willerton, "Source Localization using Large Aperture Sparse Arrays," IEEE Trans. Signal Processing, November 2012.
- [2] M. Willerton, Y.I. Kamil and A. Manikas, "Auto-Calibration of Sparse Arrays of Sensors," IEEE Trans. Antennas and Propagation (under review).
- [3] M. Willerton, K. Stavropoulos and A. Manikas, "*Pilot Based Array Calibration in the Presence of Sensor Uncertainties*," Trans. Antennas and Propagation (under review).
- [4] M. Willerton and A. Manikas, "Array Shape Calibration using a Single Multi-Carrier Pilot," Signal Sensor Processing for Defence (SSPD 2011), September 2011, London, UK.
- [5] M. Willerton and A. Manikas, "Virtual Linear Array Modelling of a Planar Array," 2<sup>nd</sup> IMA Conference on Mathematics in Defence, October 2011, Swindon, UK.





- Developed a pilot based global array calibration algorithm which estimates gain, phase and sensor location uncertainties using sources at known locations operating at single or multiple frequencies
- Devised a novel array autocalibration algorithm which allows the array to calibrate itself assuming array elements can operate as transceivers
  Successfully devised methods to track the shape of a towed array using
- eigenvector methods and state space approaches. Future scope is to investigate how to opportunistically exploit the flexible array.



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